



# Interference Management for Multiuser Two-Way Relay Networks

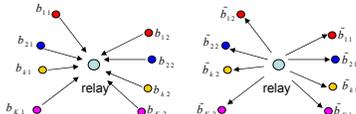
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## Multiuser Two-Way Relay Networks

- Two-way relaying outperforms traditional "one-way" relaying
- In wireless ad hoc networks:
  - it is likely that we have **many more than two nodes**
  - there are **shared** intermediate relay(s)

**Proposal: Multiuser two-way relaying:**  
multiple pairs of partners communicate via a single relay



Phase 1: users transmit to relay Phase 2: relay broadcasts to users

## Multiple Access Method

- Employ CDMA to support multiple users:
  - Conventional design: distinct signatures for all users in the system.

**New insight:**  
utilize the bi-directional communication structure

- Each pair of partners **share** a common signature
- Only **K** signatures are needed for **2K** users.

## Objective

- Interference limited two-way relay system

**Objective:**

- Interference management by jointly optimizing
  - Transmit power levels
  - Multiuser receivers at the relay and the users
  - Relaying scheme

**Results:**

- Multiple Access Interference (MAI) is greatly reduced.
- More user pairs can be supported.

## Communication in Phase I

- Communication in Phase I:
  - The  $i^{\text{th}}$  pair of users share the common signature  $S_i$
  - Binary user symbols:  $b_{i1}, b_{i2} \in \{-1, +1\}$
  - Received signal at the relay:  $r_i = \sum_{j=1}^K (\sqrt{p_{i1}} b_{i1} + \sqrt{p_{i2}} b_{i2}) S_i + n_i$

How does the relay forward the information?

**Jointly demodulate-and-XOR-forward (JD-XOR-F) relaying**

- Upon receiving  $r_i$ , the relay will
  - employ a linear filter to obtain  $y_i = c_i^T r_i$
  - generate  $\hat{b}_i \in \{-1, 1\}$ , the estimate of  $b_i = b_{i1} \oplus b_{i2}$
  - spread  $\hat{b}_i$  with  $S_i$ , and broadcast K symbols simultaneously

$$\mathbf{x}_0 = \sum_{i=1}^K \sqrt{p_{0i}} \hat{b}_i S_i$$

## Decision Rule in Phase I

- Relay decides in favor of two hypothesis: whether two partners have sent the same symbol or not

$$\hat{b}_i = -1 \text{ when } b_{i1} = b_{i2}; \hat{b}_i = 1 \text{ otherwise}$$

No closed-form solution unless equal received power per pair is employed.

- Near-optimum decision rule

- Step 1:  $(\hat{b}_{i1}, \hat{b}_{i2}) \in \{(-1, -1), (-1, 1), (1, -1), (1, 1)\}$
- Step 2:  $\hat{b}_i = \hat{b}_{i1} \oplus \hat{b}_{i2}$

- Decision rule:

$$\hat{b}_i = \begin{cases} 1, & \text{when } y_i \in R = \{y_i \mid -y_{th} < y_i < y_{th}\} \\ -1, & \text{when } y_i \in R_c \end{cases}$$

where  $y_{th} = \sqrt{q_{i1}}$  when  $q_{i1} \geq q_{i2}$ , and  $y_{th} = \sqrt{q_{i2}}$  otherwise.

## Communication in Phase II

- Received signal at terminal  $m$  ( $i=1, \dots, K, m=1, 2$ ):

$$r_{im} = \sqrt{h_{im}} x_0 + n_{im} = \sqrt{h_{im}} \left( \sum_{j=1}^K \sqrt{p_{0j}} \hat{b}_j S_j \right) + n_{im}$$

- Upon receiving  $r_{im}$ , the terminal will

- employ a linear filter to obtain  $y_{im} = c_{im}^T r_{im}$
- generate  $\hat{b}_{im}$ , the estimate of  $\hat{b}_i$
- perform an XOR operation on  $\hat{b}_{im}$  and  $b_{im}$  to recover the partner's symbol.

**The unique feature of two-way communication:**

Each user utilizes the side information (its own symbol) to subtract the self-interference from the signal broadcasted by the relay.

## Interference Management Problem

- Optimum interference management for each phase:  
We seek to expend the minimum total transmit power while satisfying the QoS requirements

$$\min_{\{p_{i1}, p_{i2}, c_i\}} \sum_{i=1}^K (p_{i1} + p_{i2}) \quad \text{Phase I QoS requirements}$$

$$\text{s.t. } Pe_{i1} \leq \rho_{i1} \quad \text{Phase II QoS requirements}$$

$$p_{i1} \geq 0, p_{i2} \geq 0, c_i \in \mathfrak{R}^N, \forall i$$

$$\min_{\{p_{0i}, c_{0i}\}} \sum_{i=1}^K p_{0i}$$

$$\text{s.t. } Pe_{2,1} \leq \rho_{2,1}, Pe_{2,2} \leq \rho_{2,2}$$

$$p_{0i} \geq 0, c_{0i} \in \mathfrak{R}^N, c_{0i} \in \mathfrak{R}^N, \forall i$$

Phase I: Users  $\rightarrow$  Relay (Uplink)

Phase II: Relay  $\rightarrow$  Users (Downlink)

## Interference Management Solution

**Key:** the BER constraint can be converted to the received SIR constraint in each phase

- Phase I: (more involved)

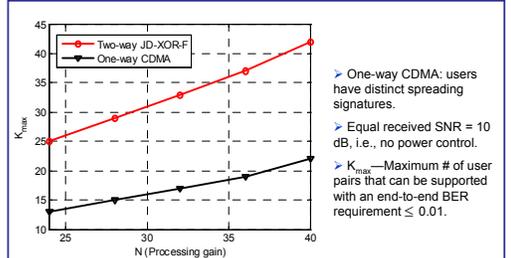
- Solve the power control subproblem for the  $i^{\text{th}}$  user pair
- Find a **sufficient condition** on the received SIRs for  $Pe_{i1} \leq \rho_{i1}$ , with the **minimum total transmit power requirement** on the  $i^{\text{th}}$  user pair

- Phase II: (more straightforward)

- One-to-one mapping between BER and SIR

The iterative power control and receiver optimization algorithm can then be implemented in each phase, and converges to its corresponding minimum power solution.

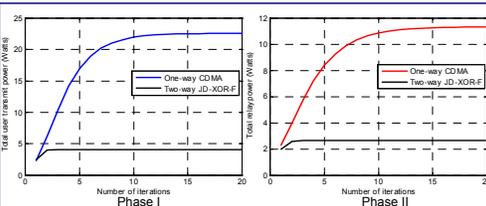
## Maximum Number of User Pairs Can be Supported



- One-way CDMA: users have distinct spreading signatures.
- Equal received SNR = 10 dB, i.e., no power control.
- $K_{\text{max}}$  — Maximum # of user pairs that can be supported with an end-to-end BER requirement  $\leq 0.01$ .

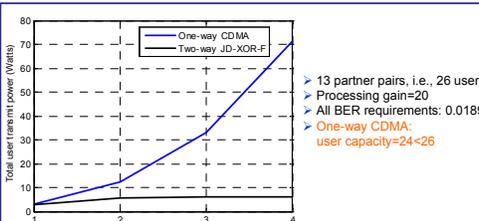
The multiuser two-way JD-XOR-F relaying almost **doubles** the numbers of user pairs that can be supported by the "one-way" CDMA relaying.

## Total Power with Iterative Power Control



- Iterative power control and receiver updates
  - Total transmit power is minimized.
- Two-way JD-XOR-F relaying achieves significant power savings.

## Overloaded System in Phase I



- One-way CDMA  $\rightarrow$  Infeasible power control problem
- Two-way relaying scheme still has a feasible solution
  - Benefit of considering the two-way communication structure

## Conclusions

- Resource sharing in two-way communications differs from that of one-way communications.
- Interference can be managed using power control, multiuser detection and the appropriate relaying scheme.
- Optimum physical layer is designed by using iterative power control and multiuser detection updates with guaranteed convergence to the optimum.
- Taking into account the bi-directional nature of communication leads to significant power savings.